

**Bilad Alrafidain University College**  
**Electric Power Techniques Engineering Department**  
**Control Systems Analysis**  
**Fourth Stage**  
**Academic Year 2020 - 2021**

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# Control Systems Analysis

## Course Contents

- Introduction to Control System.
- Transfer Function.
- Time Domain Analysis.
- Stability Analysis.
- Root Locus Method.
- Frequency Domain Analysis.
- Compensator Lead Network.
- Compensator Lag Network.
- PID Controllers.
- State Space Theory.
- State Space Representation.

## Lecture Four

# Transfer Function

## Tutorial lecture about poles and zeros

**Example 1:** Find the Poles & Zeros for the following Transfer Function and then plot them on the ( S-Plane )?

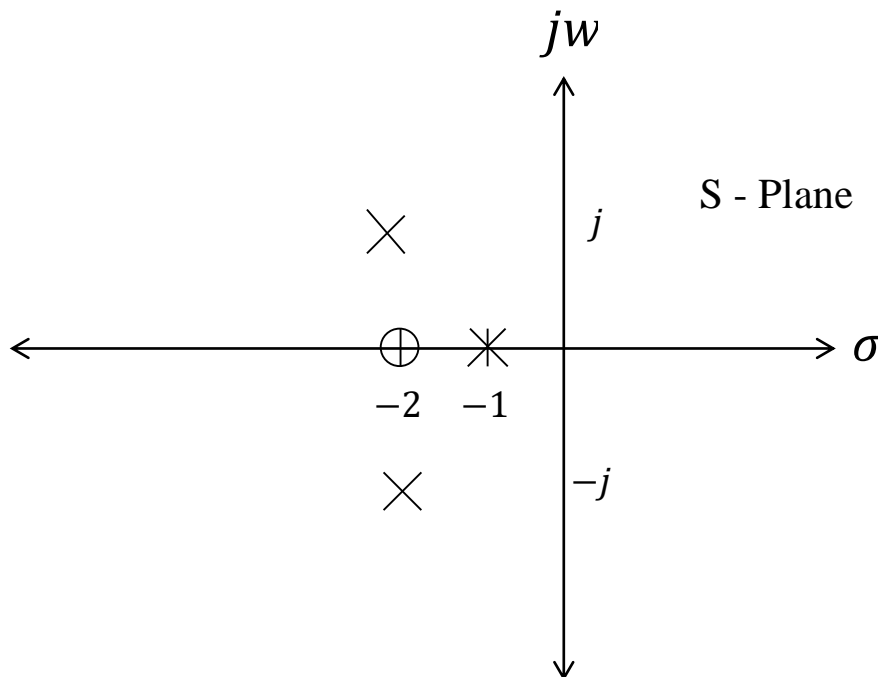
$$G(S) = \frac{(s + 2)}{(s + 1)(s + 2 + j)(s + 2 - j)}$$

**Solution:**

Zeros:  $s = -2$

Poles:  $s = -1, s = -2 - j, s = -2 + j$

Let us now draw the ( Pole – Zero Diagram ) which is a plot on ( S-plane ) represents the locations of Poles and Zeros of a Transfer Function. In the ( Pole – Zero Diagram ) the Poles are represented by ( X ) and the Zeros represented by ( O ).



**Example 2:** Find the Poles & Zeros for the following Transfer Function and then plot them on the ( S-Plane )?

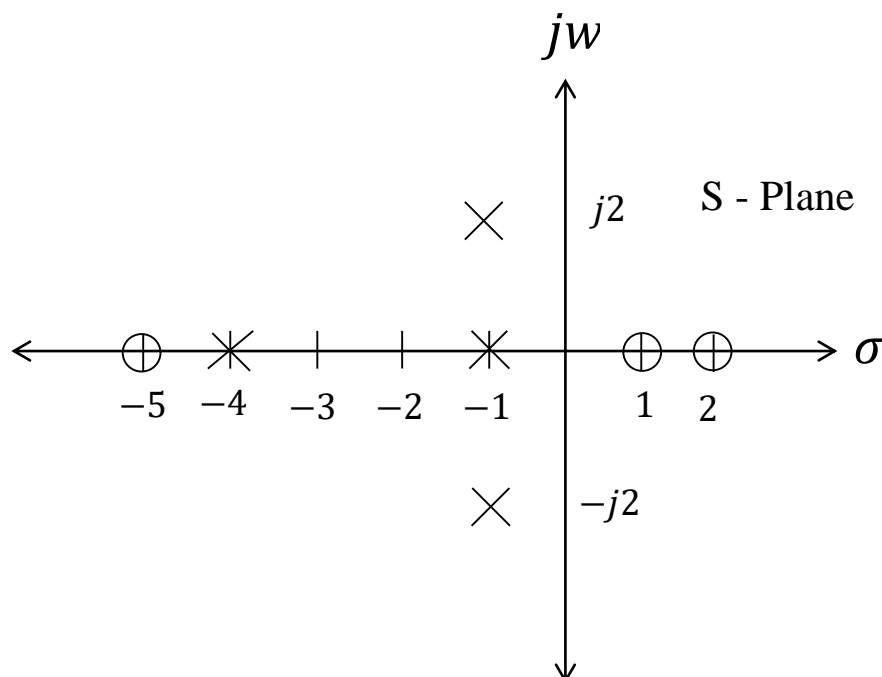
$$G(S) = \frac{(s - 1)(s - 2)(s + 5)}{(s + 4)(s + 1 + 2j)(s + 1 - 2j)}$$

**Solution:**

Zeros:  $s = 1, s = 2, s = -5$

Poles:  $s = -4, s = -1 - 2j, s = -1 + 2j$

Let us now draw the ( Pole – Zero Diagram ) which is a plot on ( S-plane ) represents the locations of Poles and Zeros of a Transfer Function. In the ( Pole – Zero Diagram ) the Poles are represented by ( X ) and the Zeros represented by ( O ).



**Example 3:** Find the Poles & Zeros for the following Transfer Function and then plot them on the ( S-Plane )?

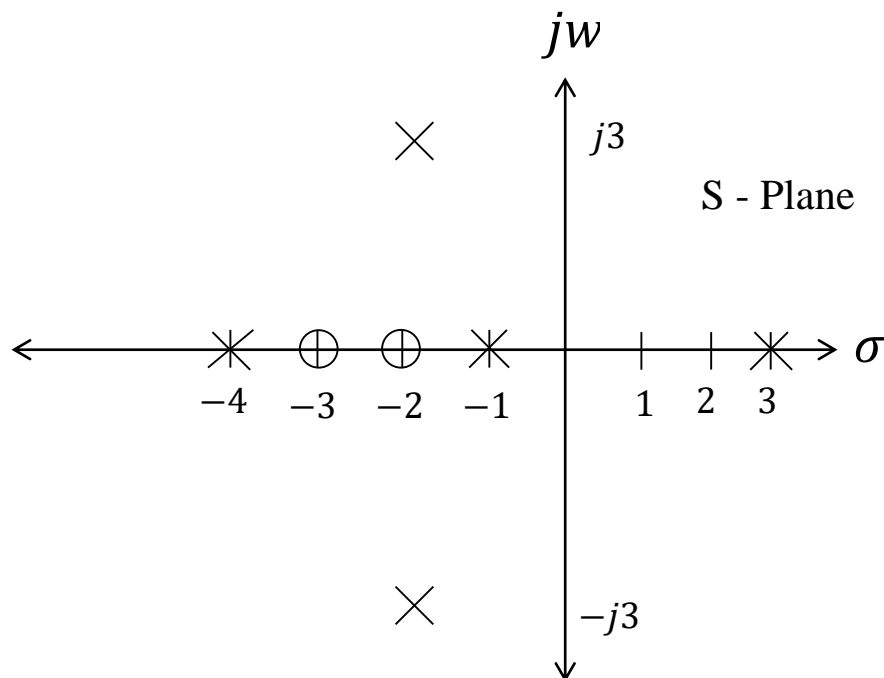
$$G(S) = \frac{(s + 3)(s + 2 + 3j)(s + 2 - 3j)}{(s - 3)(s + 1)(s + 4)}$$

**Solution:**

Zeros:  $s = -3, s = -2 - 3j, s = -2 + 3j$

Poles:  $s = 3, s = -1, s = -4$

Let us now draw the ( Pole – Zero Diagram ) which is a plot on ( S-plane ) represents the locations of Poles and Zeros of a Transfer Function. In the ( Pole – Zero Diagram ) the Poles are represented by ( X ) and the Zeros represented by ( O ).



**Example 4:** Find the Poles & Zeros for the following Transfer Function and then plot them on the ( S-Plane )?

$$G(S) = \frac{(s + 1)(s - 2)(s + 3)(s - 4)}{(s - 1)(s + 2)(s - 3)(s + 4)}$$

**Solution:**

Zeros:  $s = -1, s = 2, s = -3, s = 4$

Poles:  $s = 1, s = -2, s = 3, s = -4$

Let us now draw the ( Pole – Zero Diagram ) which is a plot on ( S-plane ) represents the locations of Poles and Zeros of a Transfer Function. In the ( Pole – Zero Diagram ) the Poles are represented by ( X ) and the Zeros represented by ( O ).

